## CMPE 350 - Spring 2019

## PS 8 - 08.04.19

**3.5** Examine the formal definition of a Turing machine to answer the following questions, and explain your reasoning.

- a) Can a Turing machine ever write the blank symbol on its tape?
- **b**) Can the tape alphabet  $\Gamma$  be the same as the input alphabet  $\Sigma$ ?
- c) Can a Turing machine's head ever be in the same location in two successive steps?
- d) Can a Turing machine contain just a single state?

3.7 Explain why the following is not a description of a legitimate Turing machine.

 $M_{\text{bad}} =$  "On input  $\langle p \rangle$ , a polynomial over variables  $x_1, \ldots, x_k$ :

- 1. Try all possible settings of  $x_1, \ldots, x_k$  to integer values.
- 2. Evaluate p on all of these settings.
- 3. If any of these settings evaluates to 0, accept ; otherwise, reject."

• Design a context-free grammar whose language contains a string which has infinitely many derivations.

• Prove that a PDA that has the ability to reverse the contents of its stack is more powerful than the ordinary PDA.

• Some questions from old exams.