

## CMPE 350 - Spring 2019

### PS 3 - 04.03.19

- Prove: "If a DFA with  $n$  states accepts a string of length  $n - 1$ , then it also accepts infinitely many other strings."

**1.29** Use the pumping lemma to show that the following languages are not regular.

b)  $A_2 = \{www | w \in \{a, b\}^*\}$

c)  $A_3 = \{a^{2^n} | n \geq 0\}$

- Show that  $L = \{010^n 1^n | n \geq 0\}$  is not regular.

**1.46** Prove that the following languages are not regular. You may use the pumping lemma and the closure properties of the class of regular languages under union, intersection and complement.

a)  $L = \{0^n 1^m 0^n | m, n \geq 0\}$

b)  $L = \{0^m 1^n | m \neq n\}$

c)  $L = \{w | w \in \{0, 1\}^* \text{ is not a palindrome}\}$

**1.54** Consider the language  $F = \{a^i b^j c^k | i, j, k \geq 0 \text{ and if } i = 1, \text{ then } j = k\}$

- a) Show that  $F$  is not regular.

**1.38** An all-NFA  $M$  is a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$  that accepts  $x \in \Sigma^*$  if every possible state that  $M$  could be in after reading input  $x$  is a state from  $F$ . Note, in contrast, that an ordinary NFA accepts a string if some state among these possible states is an accept state. Prove that all-NFAs recognize the class of regular languages.

- Some questions from old exams