CMPE 300 – Analysis of Algorithms Fall 2016 Assignment 1

Due: November 11, 17:00

This is an individual homework. Please answer the following questions and submit your answers to your assistant as hard copy. The sole purpose of this homework is to familiarize you with the processes involved in answering complexity related questions. Please work on them by your own. Please do not submit just an answer, but show all your reasoning, and how you arrive at the answers. For any further questions, contact the assistant.

Question 1 (50 points)

SortDesc algorithm takes an array with n elements and sorts the elements in descending order. Assume n is a positive power of 2.

- Write the complexity of this algorithm T(n) as a recurrence relation. (15 Points)
- Solve the recursion and find the exact complexity, then state the complexity in big O notation. (35 Points)

```
procedure SortDesc(A[0:n-1]) recursive
input:
                 A[0:n-1]
                                  (an array of integers with size n)
output:
                 A[0:n-1]
                                  (array altered by procedure)
if n = 2 then
        tempVar \leftarrow -1
        if A[0] < A[1] then
                 tempVar \leftarrow A[0]
                 A[0] \leftarrow A[1]
                 A[1] \leftarrow tempVar
        endif
else
        m \leftarrow n/2
         for i \leftarrow 0 to m-1 do
                 Temp1[i] \leftarrow A[i]
                 Temp2[i] \leftarrow A[i+m]
         endfor
        SortDesc(Temp1)
        SortDesc(Temp2)
        i \leftarrow 0
        i \leftarrow 0
        k \leftarrow 0
        while i < m or j < m
                 if i = m
```

```
Temp3[k] \leftarrow Temp2[j]
                  j \leftarrow j+1
else if j = m
                           Temp3[k] \leftarrow Temp1[i]
                           i \leftarrow i + 1
                  else if Temp1[i] < Temp2[j]
                           Temp3[k] \leftarrow Temp2[j]
                           j \leftarrow j + 1
                  else
                           Temp3[k] \leftarrow Temp1[i]
                           i ← i + 1
                  endif
                  k \leftarrow k + 1
         endwhile
         for i \leftarrow 0 to m-1 do
                  A[i] \leftarrow Temp3[i]
         endfor
endif
```

Question 2 (50 Points)

Consider the given function f(n) and determine whether the following cases are true or false. Justify your answers formally ie. show all your work in deriving your answer. (Hint: Use Stirling's Approximation)

$$f(n) = n^4 + n * \log(5n! * n^4) + n^2\sqrt{n} + 42$$

- 1. $f(n) \in O(n^6)$ (10 Points)
- 2. $f(n) \in o(n^5)$ (15 Points)
- 3. $f(n) \in \Omega(n^3 * log(n))$ (10 Points)
- 4. $f(n) \in \Theta(n^5 * log(n))$ (15 Points)