

Computer Vision

Segmentation: boundary based techniques, continued
Model based approaches in boundary detection

Boundary based segmentation

- Deformable templates
- Snakes
- Active Countours
- Active Shape Models

Deformable templates

- Parametric shape models with few degrees of freedom $r(s, X)$
- Match the template to an image by searching for the value of X that minimizes an external energy term, $E_{\text{ext}}(X)$
- An internal energy term, $E_{\text{int}}(X)$ can be included as a "regularizer" .

Snakes

- We are given a feature map, $F(r)$
- Treat - gradient of $F(r)$ as a landscape on which the snake, $r(s)$ $0 < s < 1$ can slither
- Maximize $\text{grad } F(r(s))$ while retaining smoothness of the snake

$$\underbrace{\left(\frac{w_1 \partial r}{\partial s} - \frac{w_2 \partial^2 r}{\partial s^2} \right)}_{\text{Internal forces}} + \underbrace{\nabla F}_{\text{external force}} = 0$$

∇F : spatial gradient of F
 w_1 : elasticity
 w_2 : stiffness

Snakes - Discretization

- Sparse set of equations:

$$w_1 r'_s(s_1) - w_2 r''_{ss}(s_1) + \nabla F(s_1) = 0$$

$$w_1 r'_s(s_2) - w_2 r''_{ss}(s_2) + \nabla F(s_2) = 0$$

⋮

- To find out what the curve looks like in between, use polygonal approximation or splines
- If B-splines are used, the smoothness term may be omitted

Active Contours

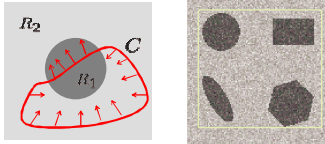
- Feature map $F(t)$ and active contour $r(s, t)$ both vary in time

$$\rho r_{tt} = - \left(\gamma r_t - w_1 \frac{\partial r}{\partial s} + w_2 \frac{\partial^2 r}{\partial s^2} \right) + \nabla F$$

ρ : mass density

γ : viscous resistance from the medium surrounding the snake

Curve Evolution (Active Contours formulated as a Bayesian problem)



- Formulate as an optimization problem for the curve C

$$\hat{C} = \arg \min_C \{E(C)\}$$
- Solve iteratively by "evolving" the curve

$$\hat{C}^{(n+1)} = \mathcal{F}(\hat{C}^{(n)})$$
- How to choose the objective functional $E(C)$?

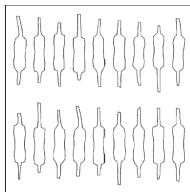
Active Shape Models Overview

- The algorithm
 - Training
 - Manually landmark shape points
 - Align the training set
 - Learn the shape variability
 - » May now generate new shapes
 - ASM
 - Iterate for optimizing the translation, rotation, scale parameters and also the shape parameters with an optimization algorithm (based for example on gradients)

ASM Overview

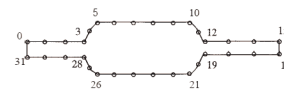
- Training set of shapes

Different resistor shapes



ASM Overview

- We wish to learn the variability of the shapes.
 → Define Landmark Points (N)



Each landmark point should be in correspondence!!

ASM Overview

- The shapes in the training set may be of different rotation, scale and translation.
 → They must be aligned to the same coordinate frame.

Generalized Procrustes Method



Iterative Least Square Optimisation for translation, rotation, scale parameters.

PROCRUSTES STEPS

1. Find centers of gravity and $\bar{\mathbf{x}}, \bar{\mathbf{y}}$
2. Form displacements

$$\bar{\mathbf{x}}_i = \mathbf{x}_i - \bar{\mathbf{x}}, \quad \bar{\mathbf{y}}_i = \mathbf{y}_i - \bar{\mathbf{y}}$$

3. Form the matrix $\mathbf{A} = \sum_{i=1}^n \bar{\mathbf{x}}_i \bar{\mathbf{y}}_i^T$
4. Obtain SVD $\mathbf{A} = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^T$

5. Take $\mathbf{Q} = \mathbf{V} \mathbf{U}^T$

6. Take $\mathbf{t} = \bar{\mathbf{y}} - \mathbf{Q} \bar{\mathbf{x}}$

ASM Overview

- Apply PCA to the training set.
 - Consider each training shape as a point in 2N space.
 - Apply PCA to the points (training shapes) in this 2N dimensional space to learn the shape variability.
 - Generate new shapes by

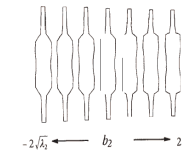
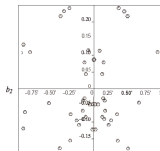
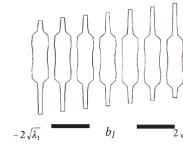
$$x = \bar{x} + Pb$$

where P: matrix of eigenvectors,
b: weights

ASM Overview

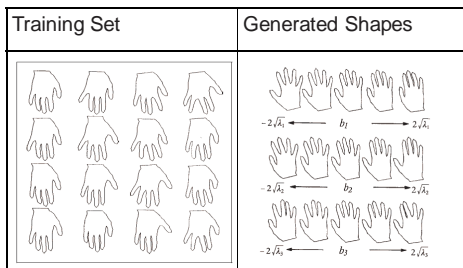
- New shapes

Eigenvalue	$\frac{\lambda_i}{\lambda_T} \times 100\%$
λ_1	66%
λ_2	8%
λ_3	5%
λ_4	4%
λ_5	3%
λ_6	3%



ASM Overview

- Another example



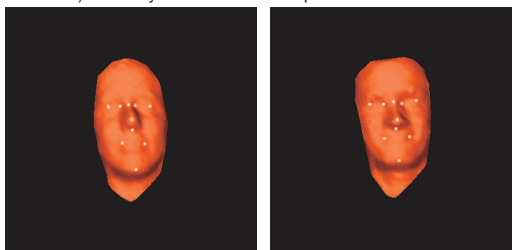
ASM Overview

- Image search (Iterative)

- Optimize translation, rotation, scale parameters
- Optimize shape parameters
- Constrain shape parameters according to training set
- Until the process converges

Automated Registration of 3D Faces using Dense Surface Models

- Learning algorithm
 - 1) Manually landmark 10 facial points.

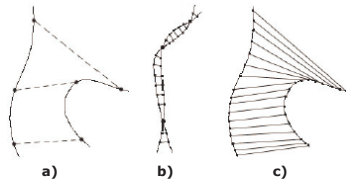


Automated Registration of 3D Faces using Dense Surface Models

- 2) Compute the mean landmarks using Generalised Procrustes analysis.
- 3) Warp the surfaces using their 10 landmark points onto the mean landmark points using the "Thin Plate Spline Warping" algorithm.
 - » TPS is a type of spline interpolation powerful in modelling biological shape changes.
 - » It simulates the shape changes of a thin metal sheet and therefore minimizes the bending energy of the transform, keeping the distortion to a minimum.

Automated Registration of 3D Faces using Dense Surface Models

- 4) Each Warped surface is resampled using a base mesh and returned to its original position.



The TPS alignment step illustrated in 2D. The surfaces are landmarked (a), then TPS warped onto a mean set of landmarks and a dense correspondence is established (b). Finally the surfaces are unwarped back to their original locations (c).

Automated Registration of 3D Faces using Dense Surface Models

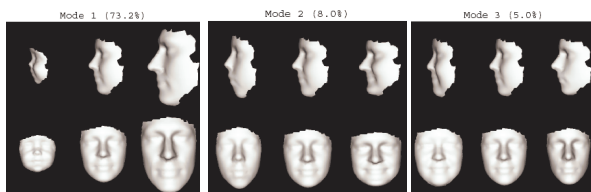
- 5) If the resampling distance exceeds a threshold, do not include these points in the landmark set.

→ Only points that appear in all shapes are included in the landmark set.

- 6) Procrustes as in ASM

- 7) PCA as in ASM.

Automated Registration of 3D Faces using Dense Surface Models



420 people. Aging from 1 to 80. Both genders. Neutral expressions.

Automated Registration of 3D Faces using Dense Surface Models

• Fitting Algorithm

- 1) Initial template $x(0)$ (mean template), target template y (test data)
- 2) ICP (Iterative Closest Point) to fit $x(0)$ to $y \rightarrow x(1)$
- 3) Closest point mapping $x(1)$ to $y \rightarrow x(2)$
- 4) Procrustes $x(2)$ onto $\bar{x}(3)$
- 5) Extract the shape coefficients b

$$b = W^{-1} \Phi^T (x(3) - \bar{x})$$

- 6) The shape parameters are limited to learned variances from the training set $\rightarrow b'$

Automated Registration of 3D Faces using Dense Surface Models

- 7) The best guess surface is computed $\rightarrow x(4)$

$$x(4) = \bar{x} + \Phi W b'$$

- 8) $x(4)$ aligned with $x(2) \rightarrow x(5)$

- 9) Iterate with $x(1)$ new = $x(5)$

ASM for facial expression recognition

- İsmail Arı

Appearance

- $Appearance = Shape + Texture$
- **Shape:** tuple of characteristic locations in the image, up to allowed transformation
 - Example: contours of the face up to 2D similarity transformation (translation, rotation, scaling)
- **Texture:** intensity (or color) patch of an image in the shape-normalized frame, up to scale and offset of values

Shape

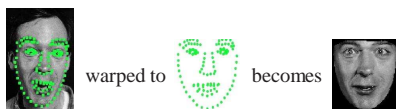
- Configuration of landmarks
 - Good landmarks – points, consistently located in every image. Add also intermediate points
 - Represent by vector of the coordinates: e.g. $x=(x^1, \dots, x^n, y^1, \dots, y^n)^T$ for n 2D landmarks
- Configurations x and x' are considered to have the same *shape* if they can be merged by an appropriate transformation T (registration)
- **Shape distance** – the distance after registration:

$$dist_{shape}(x, x') = \inf_T dist(x, Tx')$$

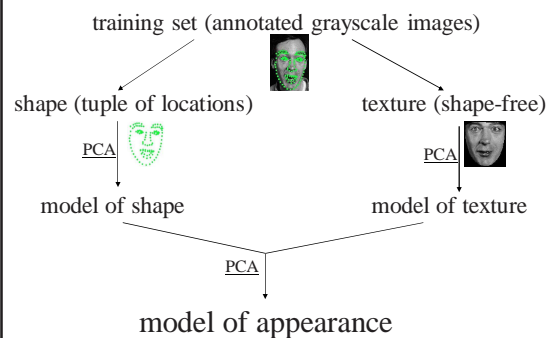


Shape-free texture

- An attempt to eliminate texture variation due to different shape ("orthogonalization")
- Given shape x and a target "normal" shape x' (typically the average one) we warp our image so that points of x move into the corresponding points of x'

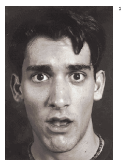


Modeling Appearance



Training set

- Annotated images
- Done manually, it is the most human time consuming and error prone part of building the models
- (Semi-) automatic methods are being developed**



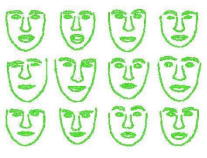
* Example from: *Active Shape Model Toolkit* (for MATLAB), Visual Automation Ltd.
 ** A number of references is given in: T.F.Cootes and C.J.Taylor. "Statistical Models of Appearance for Computer Vision", Feb 28 2001; pp. 62-65

Training sets for shape and texture models


- From the initial training set (annotated images) we obtain $\{x_1, \dots, x_n\}$ – set of shapes, $\{g_1, \dots, g_n\}$ – set of shape-free textures.
- We allow the following transformations:
 - S for the shape: translation (t_x, t_y) , rotation θ , scaling s .
 - T for the texture: scaling α , offset β ($Tg = (g - \beta\mathbf{1})/\alpha$).
- Align both sets using these transformations, by minimizing distance between shapes (textures) and their mean
 - Iterative procedure: align all $x_i(g)$ to the current $\bar{x}(\bar{g})$, recalculate $\bar{x}(\bar{g})$ with new $x_i(g)$, repeat until convergence.

Examples of training sets


Shapes



The mean shape



Textures




* From the work of Mikkel B. Stegmann, Section for Image Analysis, The Technical University of Denmark

Model of Shape

- Training set $\{x_1, \dots, x_n\}$ of aligned shapes
- Apply PCA to the training set
 - Model of shape: $x = \bar{x} + P b_s$
 where \bar{x} (the mean shape) and P_s (matrix of eigenvectors) define the model;
 b_s is a vector of parameters of the model.
 - Range of variation of parameters: $|b_s^i| \leq 3\sqrt{\lambda_i}$
 determined by the eigenvalues, e.g.

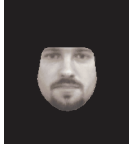
Example: 3 modes of a shape model



Model of Texture

- Training set $\{g_1, \dots, g_n\}$ of shape-free normalized image patches
- Apply PCA
 - Model of texture: $g = \bar{g} + P_g b_g$
 - Range of variation of parameters

Example: 1st mode of a texture model:



Combining two models

- Joint parameter vector $b = \begin{pmatrix} W_s b_s \\ b_g \end{pmatrix}$
 where the diagonal matrix W_s accounts for different units of shape and texture parameters.
- Training set
 - For every pair (x_i, g_i) we obtain:




$$b_i = \begin{pmatrix} W_s b_{si} \\ b_{gi} \end{pmatrix} = \begin{pmatrix} W_s P_s^T (x_i - \bar{x}) \\ P_g^T (g_i - \bar{g}) \end{pmatrix}$$
- Apply PCA to the training set $\{b_1, \dots, b_n\}$
 - Model for parameters: $b = P_c c$, $P_c = [P_{cs} | P_{cg}]^T$
 - Finally, the combined model:

$$x = \bar{x} + Q_s c, g = \bar{g} + Q_g c$$
 where $Q_s = P_s W_s^{-1} P_{cs}$, $Q_g = P_g P_{cg}$


Examples (combined model)

$$x = \bar{x} + Q_s c, g = \bar{g} + Q_g c$$

- Self-portrait of the inventor

Tim Cootes
His shape
A mode of the model
- Color model (by Gareth Edwards)



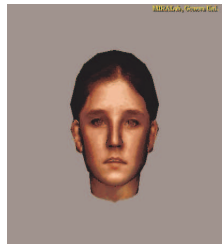
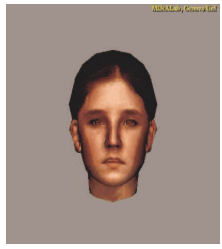
Several modes

Generating synthetic images: example

By varying parameters c in the appearance model

$$x = \bar{x} + Q_s c, g = \bar{g} + Q_g c$$

we obtain synthetic images:

Active Appearance Model (AAM)

Given:

- 1) an appearance model,
- 2) a new image,
- 3) a starting approximation

Find:

the best matching synthetic image

Approach:

- Difference vector: $\delta l = I_i - I_m$
 - I_i – input (new) image;
 - I_m – model-generated (synthetic) image for the current estimation of parameters.
- Search for the best match
 - Minimize $\Delta = |\delta l|^2$, varying parameters of the model

Predicting difference of parameters

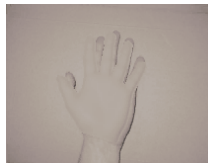
- Knowing the matching error δl , we want to obtain information how to improve parameters c
- Approximate this relation by $\delta c = \mathbf{A} \delta l$
- Precompute \mathbf{A} :
 - Include into δc extra parameters: translations, rotations and scaling of shape; scaling and offset of gray levels (texture)
 - Take δl in the shape-normalized frame i.e. $\delta l = \delta g$ where textures are warped into the same shape
 - Generate pairs $(\delta c, \delta g)$ and estimate \mathbf{A} by linear regression.

AAM search: examples

Model of face



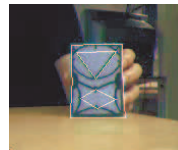
Model of hand



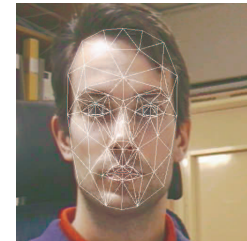
From the work of Mikkel B. Stegmann, Section for Image Analysis, The Technical University of Denmark

AAM: tracking experiments

AAM



Extension of AAM



Done with AAM-API (Mikkel B. Stegmann)

By Jörgen Ahlberg, Linköping University